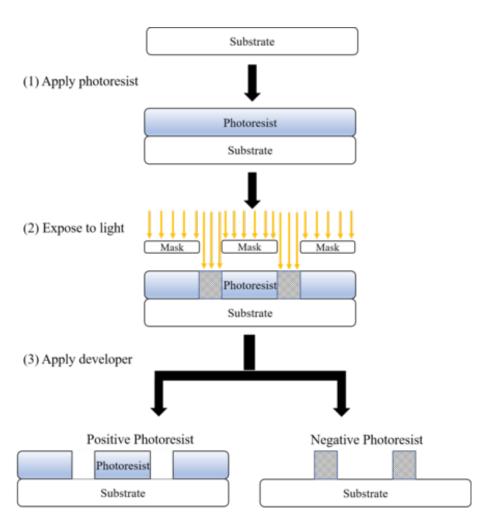
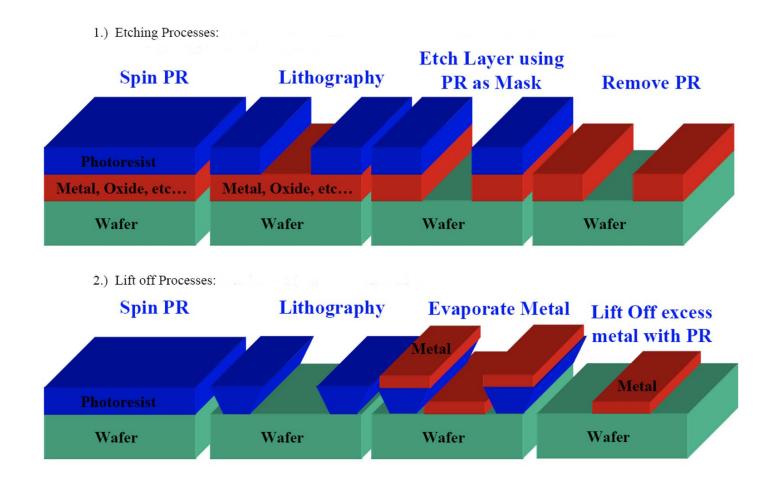




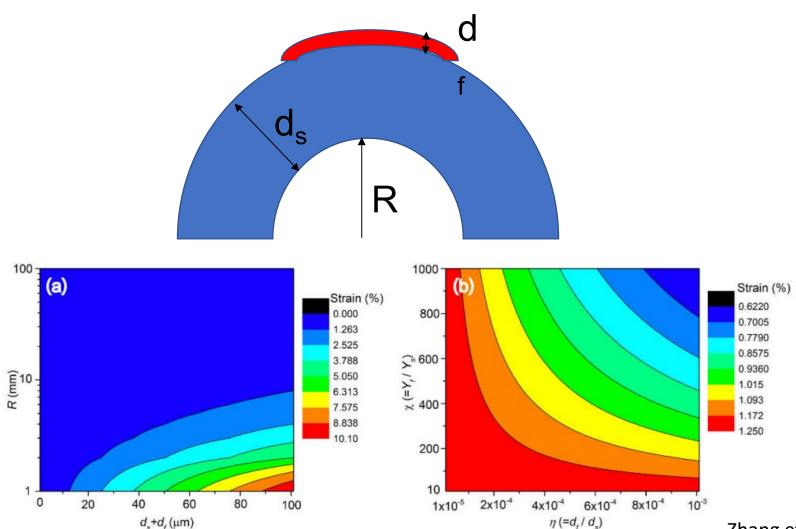
Photolithography



Etching vs Lift-Off



Bending of plastic foils



$$\varepsilon = \frac{d_s + d_f}{2R}$$
For thin films
$$d_s > d_f$$

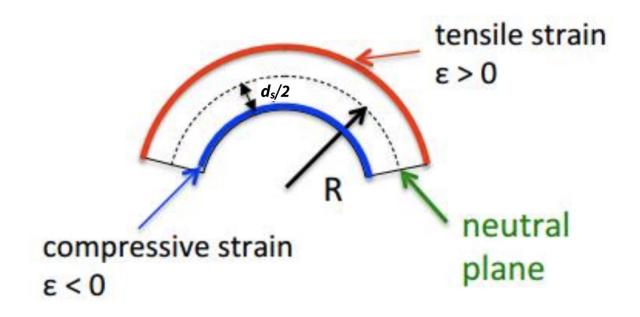
$$\varepsilon = \frac{d_s}{2R}$$

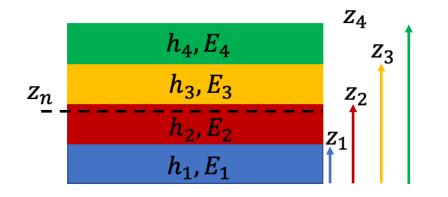
Y_f = film Young's modulus Y_s = substrate Young's modulus d_f = film thickness d_s = substrate thickness

Zhang et al. 2017

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Neutral plane and bending in multilayers





$$\varepsilon_i = \frac{z_i - z_n}{R}$$

$$\sigma_i = E_i \varepsilon_i$$

$$z_n = \frac{\sum_{i=1}^N \overline{E}_i h_i \overline{z}_i}{\sum_{i=1}^N \overline{E}_i h_i}$$

$$\overline{E}_i = \frac{E_i}{(1 - v^2)}$$

 E_i = Young's modulus

 h_i = layer thickness

 v_i = Poisson ratio

 \bar{E} = plane-strain modulus

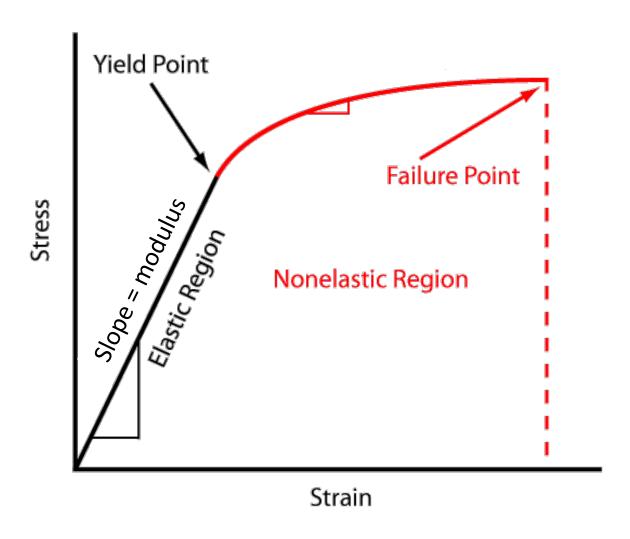
 \overline{z}_i = position of middle of layer I

 z_i = position of top of layer i

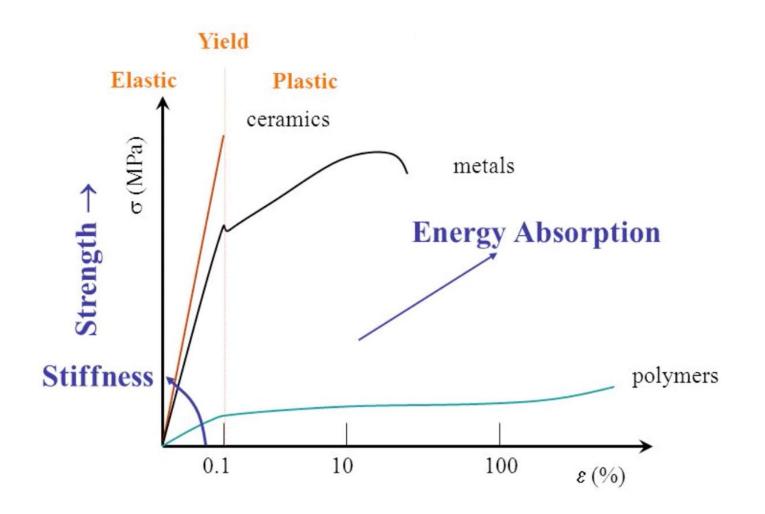
 ε_i = strain in layer i

 σ_i = stress in layer i

Tensile test on materials



Tensile test on materials



Slope: Stiff → Soft

Ultimate strength:
Strong ←→ Weak

Plastic deformation:
Brittle ←→ Ductile